# The Role of Water on Postcombustion CO<sub>2</sub> Capture by Vacuum Swing Adsorption: Bed Layering and Purge to Feed Ratio

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The influence of water vapor on the adsorption of  $CO_2$  in carbon capture by vacuum swing adsorption (VSA) was described. VSA experiments with single and multilayered columns using alumina and zeolite 13X were conducted to understand the migration of water. The penetration depth of water in the column could be controlled by maintaining the purge-to-feed ratio above a critical value. At high water content in the feed (>4%), employment of a water adsorbing prelayer was essential to prevent failure of the carbon capture process. A simple axial working capacity model predicts the penetration depth of water in the column for a given feed temperature and adsorption isotherm, and the layering ratio can be selected accordingly. Although water is detrimental to  $CO_2$  capture with polar adsorbents, long-term recovery of  $CO_2$  is still possible by appropriate layering and ensuring an adequate purge-to-feed ratio. © 2013 American Institute of Chemical Engineers AIChE J, 60: 673–689, 2014

Keywords: vacuum swing adsorption, carbon capture, water, purge-to-feed ratio, multilayered column

# Introduction

Vacuum swing adsorption (VSA) is a promising technology for capturing CO<sub>2</sub> from a variety of industrial flue gases. Previous experimental and simulation studies have shown that adsorption-based capture of CO2 from dry flue gases can be achieved with high purity (>90%) and recovery (>80%). 1-5 However, for real flue gas, the presence of heavy impurities, depending on the fuel sources, such as H<sub>2</sub>O, SO<sub>x</sub>, NO<sub>x</sub> and so forth, may severely affect the CO<sub>2</sub> capture process.6,7 Particularly, flue gas is invariably saturated with water (3-10%) and is, therefore, the major "impurity," significantly lowering the adsorption capacity of CO<sub>2</sub> on polar adsorbents, such as most of the zeolites<sup>8</sup> and metal organic frameworks.<sup>9</sup> Some aminosilica materials<sup>10,11</sup> such as amine tethered or polyethyleneimine impregnated mesoporous silica show considerable CO2 uptake in the presence of water vapor; however, owing to the chemisorption nature, the long-term chemical stability and regenerability of the aminosilica materials<sup>12</sup> not yet comparable to the benchmark 13X zeolites under VSA conditions. Nevertheless, CO2 adsorption capacity on 13X zeolite is extremely vulnerable to water vapor.<sup>13</sup> Because of its large dipole moment, water bonds strongly with the cations in zelites, characterized by a high

position. Layered columns have been used in pressure swing

adsorption (PSA) processes for several applications, such as:

heat of adsorption (e.g., >50 kJ/mol on zeolite 13X). There

have been many published works on the removal of both

water vapor and CO<sub>2</sub> by adsorption processes, but they are

confined to the field of air prepurification, where the concentration of CO<sub>2</sub> is limited to ppm levels. <sup>14,15</sup> One exception is

the recent simulation work by Ribeiro et al. 16 regarding the

effect of water vapor on purification of the light component

H<sub>2</sub>. However, process study on the recovery of heavy com-

ponents (CO2 in this case) from humid gases is still rare in

literature. Our preliminary work suggested that simultaneous

carbon capture and water removal can be integrated with a

single VSA unit, which is believed more cost competitive

than that using predrying stage.<sup>6</sup> However, in that work,

only a single adsorbent layer (13X) was used to treat flue gases with low water content. Most importantly, the key fac-

tors controlling the CO<sub>2</sub>/H<sub>2</sub>O concentration profiles and their

interactions in the column remain unresolved. It is challeng-

ing to capture CO<sub>2</sub> from gases with even higher water con-

tent (>4% v/v) which may prevail at real flue gas

temperatures.

Conversely, as few adsorbents work equally well for all gas components, adding a prelayer for water removal seems necessary for protecting the  $CO_2$  adsorption layer. Using a layered bed configuration is not a new concept in adsorption-based technologies. <sup>15,17–28</sup> The advantage of using a multilayered column over multicolumns in series is clear in that it reduces the capital cost. Furthermore, the proportion of the layers can be adjusted according to the feed com-

Additional Supporting Information may be found in the online version of this article.

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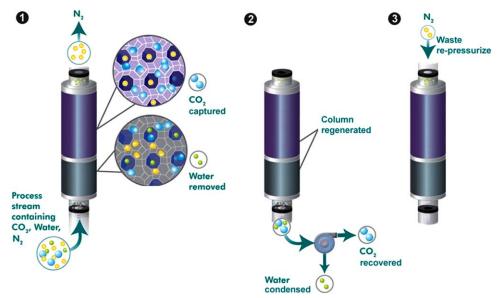


Figure 1. Three step cycle design for CO<sub>2</sub>/H<sub>2</sub>O VSA with double/multilayered layered column: step 1, adsorption; step 2, countercurrent evacuation; step 3, repressurization.

(1) air prepurification, <sup>14,15,21</sup> with an activated alumina layer to remove mainly H<sub>2</sub>O followed by a zeolite layer to remove CO<sub>2</sub> (ppm level) and the other components, in which an extra catalyst layer can be added in between to convert the trace hydrocarbons and carbon monoxide into CO2 and water and get removed by the subsequent zeolite layers; <sup>29</sup> (2) H<sub>2</sub> purification; <sup>23–25,28</sup> (3) upgrading methane from CH<sub>4</sub>/CO<sub>2</sub>/N<sub>2</sub> mixtures. <sup>18,19</sup> Moreover, layered columns were also used in temperature swing adsorption for air drying. <sup>17,30</sup> The general principle of using a layered bed involves using a weak adsorbent with a more linear isotherm (e.g., activated carbon) and hence larger working capacity to remove the bulk impurity at the inlet of the bed followed by a strong adsorbent with favorable isotherm to eliminate the residual traces.15

Also, optimization of the ratio of the column layers is important for maximizing the use of each adsorbent and minimizing the adsorber size. This optimal ratio is normally determined by comparing the performance of the system over a range of experiments/simulations at certain constraints under specific operation conditions, <sup>15,17,23,25</sup> for example, the requirement of a minimum product purity. Nikolić et al. developed a strategy, named state transition network representation, to optimize multilayered PSA processes.<sup>31</sup> Chlendi and Tondeur<sup>20</sup> studied the dynamics and optimization of layered columns in PSA with a pseudo-characteristics method and they discovered that the transfer of the concentration waves from one layer to the other showed phenomena of refraction, diffraction, dispersion, and interference similar to light rays in optics. Pigorini and LeVan<sup>32</sup> solved the periodic concentration profile and the penetration depth of the shock wave in layered isothermal PSA by using local equilibrium

All the above work involves the purification of the light products (H<sub>2</sub>, CH<sub>4</sub>, or air) harvested from the top of the column, with little concern on the heavy components. In this work, we focus on the recovery rate and purity of the heavy CO<sub>2</sub> with simultaneous removal of H<sub>2</sub>O from the bottom of the column. Therefore, a different process design is required. One typical issue is that the conventional light component purge step16 normally used for column regeneration is inappropriate in this work as it will dilute the heavy product CO<sub>2</sub>; instead, an "internal purge" can be highly desirable for sweeping off the heavier contaminant  $H_2O$ .

The aim of this study is to understand the controlling factors on the formation, migration, and stabilization of the water concentration front and to develop a convenient model to determine the penetration depth of water in a typical CO<sub>2</sub> VSA column. This study was carried out experimentally with a variety of single/multilayered columns. A number of adsorbents were tested as the H<sub>2</sub>O-removal prelayer in combination with zeolite 13X as the CO<sub>2</sub>-capture layer. The axial concentration and thermal profiles were examined to interpret the water front. Additional efforts were paid to the determination of purge-to-feed ratio and the optimization of layer ratios. Principal experimental results were further compared with our supplemental computer simulations.

#### **Experimental Work**

As shown in Figure 1, we adopted a simple three-step cycle for the VSA process: adsorption (45 s), countercurrent evacuation (variable time), and repressurization (3 s). The evaluation criteria, namely CO2 recovery, purity, and productivity were defined as usual.<sup>6</sup> The operating conditions, layering patterns, and the performance of all the experiments are summarized in Table 1.

The VSA apparatus of this work was an upgraded version of the one used in our previous studies,<sup>6</sup> with 11 thermocouples (tagged as  $T_1, T_2, \dots, T_{11}$ ) measuring the column axial temperatures. The corresponding locations of these thermocouples from bottom to top of the column were Z = 0.035 $(T_1)$ , 0.105  $(T_2)$ , 0.175  $(T_3)$ , 0.246  $(T_4)$ , 0.316  $(T_5)$ , 0.386  $(T_6)$ , 0.456  $(T_7)$ , 0.526  $(T_8)$ , 0.679  $(T_9)$ , 0.832  $(T_{10})$ , 0.984  $(T_{11})$ , respectively, where Z is the dimensionless length based on 570 cm of the total adsorbent packed column.

Table 1. Summary of Experimental Operating Conditions and Results for CO<sub>2</sub>/H<sub>2</sub>O VSA with Single and Layered Columns, respectively

				)					)	•		•		
			Layer Content and Dim	ant and Dimensionless Length Z	Length Z	Feed	Feed y <sub>i</sub> (%)	Flow			Desorp.	Rec.	Pur.	Productivity
Run No.	$^{7}$	Feed Conditions	First layer	Second layer	Third layer	CO <sub>2</sub>	H <sub>2</sub> O	- Rate (LPM <sup>a</sup> )	$P_{ m high}$ (kPa)	$P_{\mathrm{low}}$ (kPa)	Time (s)	CO <sup>2</sup> (%)	CO <sub>2</sub> (%)	(kgCO <sub>2</sub> /h/L Adsorbent)
1	20	Dry CO <sub>2</sub> in air	13X, Z(0,1)	1	1	11.2	1	99	116	2.9	112	82	73.6	0.317
2	30	Dry $CO_2$ in air	13X, Z(0,1)	ı	ı	10.7	ı	71	120	2.3	112	78.5	69	0.287
3	30	Wet 53.2% RH	13X, Z(0,1)	ı	ı	10	1.89	89	120	2.5	112	73.4	53	0.240
4	30	Wet 76.6% RH	13X, Z(0,1)	ı	I	10	2.73	89	119	5.6	112	71.7	57	0.235
S	30	Wet 96.8% RH	13X, Z(0,1)	1	1	11	3.48	89	118	2.9	112	68.2	58.5	0.246
9	30	Wet 94.6% RH	13X, Z(0,1)	ı	I	12	3.4	63	118	3.9	112	60.4	72	0.220
7	30	Wet 97.4% RH	13X, Z(0,1)	ı	I	10.7	3.5	69	119	3.2	112	89	59	0.242
,	;	112 s desorp.	:			!	,			,		į		
∞	30	Wet 97.4% RH	13X, Z(0,1)	1	1	10.7	3.5	68.7	118	3.8	100	61	27	0.234
6	30	100 s desorp. Wet 97.4% RH	13X, Z(0,1)	I	I	10.7	3.5	8.99	118	4.2	80	39	47	0.107
		80 s desorp.												
10	20	Wet 41.5% RH	13X, Z(0,1)		1	12	4.3	67.5	119	1.3	112	<4.6	39	< 0.018
11	30	Dry $CO_2$ in air,	CDX, Z(0, 0.266]	13X, Z(0.266, 1)	ı	10.7	I	70	118	2.3	112	78.5	68.5	0.183
	ć	112 s desorp.	CON COLUMN			t C	9		•	0		0	ţ	7
17	30	Wet 9/.4% KH,	CDX, Z(0, 0.266]	13X, Z(0.266, 1)	I	10.7	3.48	6.69	118	5.89	112	6.9/	/.9	0.178
13	30	Wet 97.4% RH,	CDX, Z(0, 0.266]	13X, Z(0.266, 1)	I	10.7	3.5	89	118	3.73	100	65.5	63.7	0.160
		100 s desorp.												
14	30	Wet 97.4% RH,	CDX, Z(0, 0.266]	13X, Z(0.266, 1)	I	10.7	3.48	89	118	4.47	80	58.3	62	0.165
71	30	80 s desorp.	E200 7/0 022	12 V 700 007 15		7 01		0,9	110	,	113	716	0,5	0.150
CI	30	117 c desorm	F200, <b>2</b> (0, 0.227]	13A, L(0.441, 1)	I	10.4	I	00	110	7:	711	71.0	0/	0.130
16	30	Wet 97.4% RH,	F200, Z(0, 0.227]	13X, Z(0.227, 1)	I	10.7	3.5	<i>L</i> 9	117.5	2.73	112	78.2	65	0.176
!		112 s desorp.											,	
17	30	Wet 97.4% RH,	F200, Z(0, 0.227]	13X, Z(0.227, 1)	I	10.5	3.48	89	118	3.1	100	69.4	66.5	0.167
8	30	100 s desorp. Wet 97 4% RH	F200 Z/0 02271	13X Z(0 227 1)	I	104	3 48	5.89	118.5	« «	08	583	65	0.162
)	2	80 s desorp.	[ (a)										3	
19	50	Wet 41.4% RH	F200, Z(0, 0.24]	CDX, Z(0.24, 0.52]	13X, Z(0.52, 1)	12	4.3	67.5	118	2.7	112	68.7	64.7	0.170
20	20	Wet 55.0% RH	F200, Z(0, 0.24]	CDX, Z(0.24, 0.52]	13X, Z(0.52, 1)	10.7	5.8	68.4	118.5	2.8	112	8.09	60.5	0.138
21	20	Wet 81.7% RH	F200, Z(0, 0.24]	CDX, Z(0.24, 0.52]	13X, Z(0.52, 1)	10.7	8.5	67.5	117.5	3.1	112	58.2	52.4	0.128
22	30	Dry CO <sub>2</sub> in air	F200, Z(0, 0.24]	CDX, Z(0.24, 0.52]	13X, Z(0.52, 1)	10.7	I	69	117.5	2.3	112	69.1	71.9	0.158
		,												

<sup>a</sup>Liter per minute as measured.

Table 2. Summary of Simulation Conditions and Results of Different Runs for CO<sub>2</sub>/H<sub>2</sub>O VSA with Single and Layered Columns, Respectively

			Layer Content and Dimensionless Length Z	Dimension-		Feed y <sub>i</sub> (%)				Desorn			Productivity	
Run No.	$_{({}^{\circ}C)}^{T}$	Simulation Conditions	First layer	Second layer	$CO_2$ $H_2O$	H <sub>2</sub> O	Flow Rate (LPM <sup>a</sup> )	$P_{ m high}$ (kPa)	$P_{\mathrm{low}}$ (kPa)	Time (s)	Rec. CO <sub>2</sub> (%)	Pur. CO <sub>2</sub> (%)	(kgCO <sub>2</sub> /h/L Adsorbent)	Power <sup>b</sup> (kW/ TPDCO <sub>2</sub> )
S1	30	Wet 94.6% RH	F200, Z(0, 0.227]	13X, Z (0.227, 1)	10.7	3.4	89	118	1.0	112	77.6	74.8	0.200	11.7
S2	30	Wet 94.6% RH	F200, Z(0, 0.227]	13X, Z	10.7	3.4	89	118	3.0	112	65.4	73.1	0.169	8.6
S3	30	Wet 94.6% RH	F200, Z(0, 0.227]	(0.227, 1) 13X, Z (0.227, 1)	10.7	3.4	89	118	5.0	112	48.5	69.3	0.126	9.6
S4	30	Wet 94.6% RH	F200, Z(0, 0.227]	13X, Z	0	2.73	89	118	3.0	112	0	0	0	I
S5	30	Wet 94.6% RH	F200, Z(0, 0.227]	13X, Z (0.227, 1)	35.0	3.48	89	118	3.0	112	54.0	93.6	0.4608	5.66
9S	30	Dry 0% RH	F200, Z(0, 0.227]	13X, Z (0.227, 1)	10.7	0	89	118	3.0	112	64.0	72.3	0.166	8.0
S7	30	Wet 38.7% RH	F200, Z(0, 0.227]	13X, Z (0.227 1)	10.7	1.39	89	118	3.0	112	64.5	72.5	0.167	8.8
88	30	Wet 58.1% RH	F200, Z(0, 0.227]	13X, Z (0.227, 1)	10.7	2.09	89	118	3.0	112	64.8	72.7	0.168	9.1
S9	30	Wet 77.5% RH	F200, Z(0, 0.227]	13X, Z (0.227, 1)	10.7	2.78	89	118	3.0	112	65.1	72.9	0.169	9.5

ter per minute as measured.

Another 11 gas sample ports were added at each of the thermocouple positions (Supporting Information Figure S1). The system was insulated by 1-cm thick ceramic fiber cloth, 1-cm thick nitrile rubber, and aluminium foil. A water bubbler tank was used as the humidifier with an internal heater to control the temperature. Air was humidified by adjusting the bubbler temperature and pressure, blended with pure  $CO_2$  to reach the required composition, and then transported to the buffer tank. The temperature and the partial pressure of the humid gases were analyzed by an *in situ* water sensor (HMT330, VAISALA, Finland,  $\pm 0.05\%$  full scale). All experimental control and data acquisition were managed by the Advantech® system.

Apart from the single-adsorbent layer experiments, a double-layer and a triple-layer pattern were used for the column configuration (Supporting Information Figure S1). The double-layered column used a prelayer at the bottom (inlet) of the column for water removal and a 13X main layer for CO<sub>2</sub> capture. Two commercial alumina desiccants were tested for the prelayer namely F200 (Engelhard, US) and Selexsorb® CDX adsorbent (CDX; BASF, Germany). For comparison purposes, the same mass of water adsorbent (200 g) was placed in the prelayer and the remainder of the bed was filled with 13X zeolite in each case. Detailed physical properties of the adsorbents and the column are provided in Supporting Information Tables S1 and S2. The triple-layered column consisting of F200/CDX/13X was designed for high humidity feeds (~8% v/v water), with F200 to remove bulk water, CDX to remove trace water and capture a part of the CO<sub>2</sub>, and eventually 13X to capture the majority of the CO<sub>2</sub>. VSA experiments with dry feed gases were carried out as base runs prior to the wet runs.

## **Computer Simulation**

The VSA processes were simulated with our in-house adsorption simulator to compare with the major experimental findings and investigate some process conditions that were not experimentally available. Developed by Webley and He<sup>33</sup> with FORTRAN, this well-tested simulator uses the numerical solution of the coupled mass and energy balance equations together with the viscous flow/dusty gas model to represent adsorption kinetics. The numerical method uses a solution-adaptive finite volume method with appropriate flux-limiters and is based on the additional assumptions (see Supporting Information). All the simulation conditions and results are summarized in Table 2.

# **Results and Discussion**

# Effect of purge-to-feed ratio

Purge-to-feed ratio (P/F) is a very important parameter in controlling the product purity in PSA processes. <sup>15,34–37</sup> A purge step is normally conducted by adding a portion of the light product component into the column counter-currently (i.e., from the product end) to push the concentration front of the heavy impurity components backward to "clean" the bed and avoid premature breakthrough of the heavy components on the subsequent adsorption step. <sup>34–38</sup> P/F is generally defined as the ratio of the moles of light component used in purge step to that used in the feed step regardless of step time. <sup>37,39</sup> LeVan <sup>40</sup> and, Pigorini and LeVan <sup>32</sup> defined a critical volumetric purge-to-feed ratio to characterize the minimum P/F required to keep the adsorbate contained within the

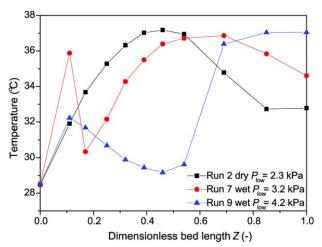


Figure 2. Axial temperature profile at the end of the adsorption step depending on dry/wet feed and vacuum pressure at 30°C of Run 2, 7, and 9.

bed at cyclic steady state (CSS). A PSA process often uses a large amount of external gases, either from the product line/ tank, or a different gas to purge the column. The gases removed during the purge step are usually disposed of as dilutes waste products. However, it is very different for CO<sub>2</sub>VSA with humid feed, in which the principal step is to recover high purity heavy components, namely CO2 and water, and regeneration of the bed is by evacuation rather than by "external" purge. As water is adsorbed at the bottom of the bed due to its highly favorable isotherm shape, all the remaining components lighter than water (CO<sub>2</sub> and air) are adsorbed in the upper layers. During the countercurrent evacuation step, the desorbed lighter components, essentially a dry gas stream, will facilitate the desorption of water by means of a so-called "internal purge" effect. 41 Therefore, the rapid change of the vacuum pressure must be taken into account in determining the forwards and backwards propagation of the water concentration front during the adsorption and desorption steps, respectively, at CSS. By reviewing the linear driving force model (see Supporting Information), 42,43 we adopted the volumetric P/F ratio for effective characterization of the repeated adsorption/desorption of water vapor in the presence of internal purge in VSA.

Case Study: VSA with Single-Layered Bed. We define the volumetric P/F ratio as the total volume of all the counter-current flow (evacuation from the bottom and backfill from the top) against the total volume of the gas flow fed to the bottom of the column. This implies both Step 2 and Step 3 are purge and only Step 1 is feed (Figure 1). However, the contribution of the repressurization step in this work can be ignored due to its small quantity (<0.5% of the feed amount).

We use the single-layered  $CO_2/H_2O$  VSA system as an example. As the cycle proceeds after startup, the length of the water loaded zone,  $Z_w$  evolves slowly to a constant value at CSS when there is no net accumulation of water in the bed. This  $Z_w$  can be determined experimentally by using the "cold spot" technique. 6,41 Corresponding to the position of the water front at a local temperature minimum, the "cold spot" is caused by the regenerative heat exchange effect due

to the abrupt change of adsorption properties in the water contaminated layer and the main CO<sub>2</sub> layer. The "cold spot" is visible in runs with wet gas (Run 7 and 9) while absent in the case of dry feed (Run 2), as can be observed from the axial temperature profiles (Figure 2). We were able to identify and plot this cold spot position  $Z_{\rm w}$  against the volumetric P/F ratio. As shown in Figure 3a, Z<sub>w</sub> increases exponentially with the decrease of P/F ratio. In the region of P/F > 1.7, water front is confined to the bottom of the bed  $(Z_w \approx 0.2)$ , indicating further withdrawal of the water front may not be worthy as it requires a rather prolonged evacuation time due to the highly favorable equilibrium isotherm of water in 13X. However, in the region of P/F < 1.7, a small reduction of P/F will lead to a sudden increase of Z<sub>w</sub>, because the migration of water front will "nibble" at the dry 13X layer used for CO2 adsorption, and in return reduce the amount of internal purge, provided by the desorbed CO2. In this region, CO<sub>2</sub> productivity, recovery, and purity fall sharply with the decrease of P/F (Figure 3b). Thus, when P/F is below a certain lower limit which we define as the critical P/F ratio<sup>32,40</sup>—approximately 1.7 in this case, water front becomes unbounded, tends to penetrate the column, and eventually destroys the CO<sub>2</sub> capture ability of the column irreversibly. Run 10 provides an example of such "creeping death." In this run, the feed water concentration was increased to 4.3% v/v, the highest humidity among all the 10 runs using a single-layered column. Eventually a water concentration of 740 ppmv was detected in the gas stream from the top of the column and no cold spot was observed, indicating penetration of the entire column by water vapor with a corresponding  $Z_w \ge 1$  (Figure 3a) in this case. The column has lost its capacity to capture CO<sub>2</sub> as reflected by a very low CO<sub>2</sub> recovery (<4.6%). It should be noted that at the end of evacuation the pressure was only 1.3 kPa-the deepest vacuum in all the runs but also the highest in terms of water partial pressure. That means no CO<sub>2</sub> was recovered from the column and the power of the pump was solely used for removing the water vapor from the column, while the P/ F ratio was as low as 0.69. Therefore, it is clear that CO<sub>2</sub> capture by VSA with a single-layered 13X column is vulnerable to the intrusion of water vapor. Any disturbance of P/F below its critical value may cause breakthrough of H<sub>2</sub>O and consequently a process failure even at a deep final vacuum (e.g., < 1.3 kPa in Run 10). Once the VSA fails, one may have to reload the column with new adsorbents, as the regeneration of wet 13X zeolite needs an elevated temperature. Nevertheless, the process failure could be avoided by operating the VSA above its critical P/F ratio with some safety margin, or by adding a prelayer specifically for water removal and protection of the main CO<sub>2</sub> adsorbing layer.

#### Effect of layering pattern

Double Layered VSA. The desired product in our VSA process is high purity  $CO_2$ . However, as a heavy component, water vapor must be prevented from breaking through the column and it is, therefore, recovered as a by-product. During the adsorption step, water is adsorbed by the bottom layer, that is, the prelayer of the column, and  $CO_2$  is adsorbed by the 13X main layer. The light components  $N_2$  and  $O_2$  quickly penetrate the column into the waste line. Owning to the large enthalpy changes of the heavy components, 44 one can readily use thermal profiles to infer  $H_2O$  and  $CO_2$  mass transfer fronts. Herein, we chose activated

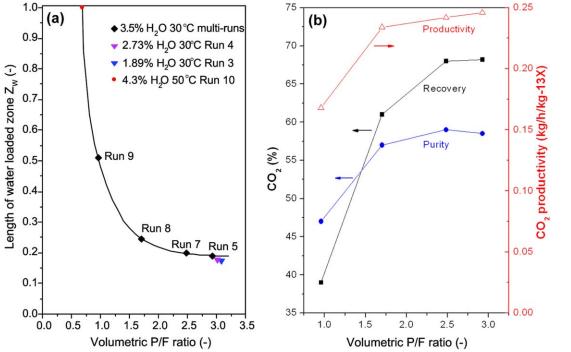


Figure 3. (a) Dependence of water loaded length on volumetric purge-to-feed ratio at CSS of single-layer 13X VSA processes.

Note: vacuum level decreases in the order of Run 5, 7, 8, 9, and 10. (b) Dependence of CO<sub>2</sub> productivity, purity, and recovery on volumetric purge-to-feed ratio at CSS of single-layer 13X VSA processes with 3.5% water feed at 30°C. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

alumina CDX and F200, respectively, as the prelayers because of their wide application in adsorption based driers. <sup>15,45,46</sup>

Figure 4 shows the complete temperature profiles of the CDX/13X double-layered column in the form of a "heat map," with dry and wet feed conditions, respectively. The heat map is a two-dimensional (2-D) evolution of the axial thermal profiles during the VSA cycle. For additional clarity, several axial profile "snapshots" were plotted in the form of conventional 2D curves (Supporting Information Figure S2) to help understand the shape and the transmission trajectory of the thermal waves. In the case of dry CO2 feed (Figure 4a), the amplitude of the temperature swing in the upper part of the column (Z = 0.7) was more pronounced than that below the layer interface due to the higher working capacity of CO<sub>2</sub> on 13X than on CDX. Moreover, during desorption stage (45 s < t < 157 s), the location of the coldest point in the column—between  $T_4$  (Z = 0.246) and  $T_5$  (Z = 0.316) at 160 s, corresponds to the location of the layer interface (Z = 0.266), indicative of the discontinuity of the heat of adsorption in the bed (e.g., for CO<sub>2</sub> adsorption,  $\Delta H_{\rm CDX} \neq \Delta H_{\rm 13X}$ ) and the formation of the cold spot even in dry gas feed (Supporting Information Figure S2a).

With wet  $CO_2$  feed (Figure 4b), there were two temperature waves propagating along the column. The broad temperature wave was attributed to the adsorption heat of  $CO_2$  in the 13X layer. The maxima of the wave was controlled to the position of  $T_9$  (Z = 0.679) with some gap to the column outlet, in order to retain the heat of adsorption within the column for providing energy to the subsequent desorption step and also improving the  $CO_2$  product purity. The other short and sharp temperature wave characterized by  $T_1$  (Z = 0.035),  $T_2$  (Z = 0.105), and  $T_3$  (Z = 0.175) was caused by water adsorp-

tion in the prelayer. We can see a distinct boundary between the two cold zones at the end of desorption step (130 s < t < 157 s), highlighted with a horizontal dashed line in Figure 4b. However, the thermal front of water reached  $T_3$  (Z = 0.175) only, suggesting  $T_4$  (Z = 0.246)—the last thermocouple in the prelayer, was still dry at CSS. The temperature profile also showed a valley around  $T_4$  (highlighted with a dashed square in Figure 4b), indicating the existence of a short zone of dry alumina CDX, which is further evidenced by the gas-phase water concentration in Figure 5.

However, in the case of wet feed with a shorter desorption time of 80 s (Figure 4c, Run 14), the temperature swing in the 13X layer was less pronounced than that in the previous cases, because of the reduced working capacity of CO2 with narrower pressure window. We found in Run 14 that the H<sub>2</sub>O thermal wave developed further into the prelayer and the wave amplitude was also greater than that of CO<sub>2</sub> in the 13X main layer because of the higher heat of adsorption of H<sub>2</sub>O on alumina. The valley between the two thermal waves (Figure 4c) was much squashed with the increase of water loaded zone but the water front was still retained within the activated alumina prelayer (Figure 5). One of the major findings from this part is that the overall performance of a double-layered VSA is superior to that using single 13X layer at wet feed conditions. Even under very harsh conditions with saturated humidity and 80 s short evacuation, our single-column VSA process using F200/13X double-layered packing could achieve a reasonable CO<sub>2</sub> recovery, purity, and productivity of 58.3%, 65%, and 0.162 kg CO<sub>2</sub>/h/Ladsorbent, respectively, whereas the corresponding performance of the VSA with single-layered 13X packing was quite poor, with only 39%, 47%, and 0.107 kg CO<sub>2</sub>/h/L-adsorbent, respectively.

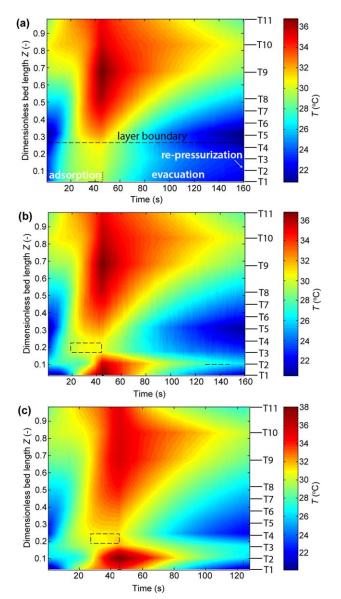


Figure 4. Axial thermal profiles of a complete cycle at CSS for CDX/13X double-layered bed during VSA at 30°C, (a) dry CO<sub>2</sub> feed in Run 11, (b) saturated CO<sub>2</sub> feed in Run 12, and (c) saturated CO<sub>2</sub> feed with shortened desorption time of 80 s in Run 14.

The dashed lines are for guidance. Vertical dashed lines represent boundaries between cycle steps. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

Triple-Layered VSA. Postcombustion flue gases are saturated at the operating temperature (higher than the above cases) of the washing tower and then remain saturated in the downstream feed lines. Any abrupt variation of environmental temperature will affect the water content of the "washed" flue gases fed to the carbon capture unit. Therefore, there is a need to design a robust layered column working effectively over a wide range of water content. For example, a longer prelayer can be used to completely remove H<sub>2</sub>O and ensure the gas entering 13X main layer is absolutely dry. However, this will cause excessive unused prelayer for the purpose of accommodating variable feed humidities, and reduce the overall CO<sub>2</sub> capture performance.

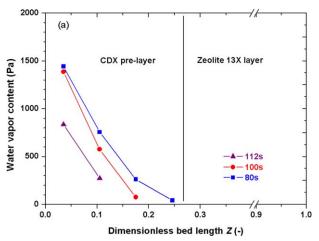


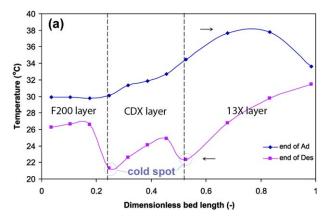
Figure 5. Water concentration profile in the gas phase in the double-layered CDX/13X VSA column at the end of the adsorption step for cycles with different desorption time: 112 s (Run 12), 100 s (Run 13), and 80 s (Run 14).

The dashed line represents the interface between the two layers. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

To overcome the above difficulty, one strategy is to add a middle layer of adsorbent with reasonable working capacity for both CO<sub>2</sub> and H<sub>2</sub>O, located in between the H<sub>2</sub>O prelayer and CO2 main layer. This middle layer can increase the robustness and flexibility of the process against variable feed compositions. Alumina CDX is a particularly good candidate for this middle layer, because CDX shows doubled CO2 capacity compared with F200 and similar quasilinear or Brunauer-Emmett-Teller (BET)-type water isotherm, exhibiting large working capacities under VSA conditions in this study (Supporting Information Figure S3). Conversely, by comparing the CO<sub>2</sub> capture performance of double-layered VSA processes using activated alumina CDX (Run 11-14) with that using F200 (Run 15-18), we can conclude F200 is marginly better than CDX as a prelayer at wet feed conditions, whereas CDX performs better at dry feed conditions owing to its larger CO<sub>2</sub> capacity.

Here, we used a F200/CDX/13X triple-layered column to treat flue gases with high water content up to 8.5% v/v. The layering ratio was preset as 0.24:0.28:0.48 (Supporting Information Figure S1b). In the case of dry CO<sub>2</sub> feed (Figure 6a), the average temperature change from the end of the adsorption step to the end of the desorption step is 3, 8, and 12°C in the F200, CDX, and 13X layers, respectively, consistent with the order of CO<sub>2</sub> working capacity on these three adsorbents. Two cold spots can be observed on the two interfaces, namely F200/CDX and CDX/13X, as a result of the discontinuity of the heat of adsorption from one layer to another. The overall performance of dry CO<sub>2</sub> feed (Run 22) was 69.1% recovery, 71.5% purity, and 0.158 kg CO<sub>2</sub>/h/L-adsorbent productivity, slightly less but still comparable to that in a single layered 13X column.

In the case of wet  $CO_2$  feed, the largest temperature change of up to  $22^{\circ}C$  occurred in the first F200 prelayer, due to the large heat of adsorption of  $H_2O$  (Figure 6b). Meanwhile, as a result of reduced vacuum level in the presence of water, both the temperature changes of the CDX



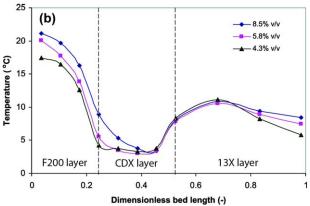


Figure 6. (a) Thermal profiles in triple-layered column with dry CO<sub>2</sub> feed at CSS in Run 22 at the end of adsorption and desorption step, respectively.

(b) Temperature changes ( $\Delta T$ ) in the triple-layered columns measured by individual thermocouples in a single cycle at CSS for wet CO<sub>2</sub> feed at different water concentrations: 4.3% v/v (Run 19), 5.8% v/v (Run 20), and 8.5% v/v (Run 21). The layer interface of F200/CDX is at Z=0.24 and CDX/13X interface at Z=0.52. Arrows represent gas flow directions. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

middle layer and the 13X main layer decreased in comparison with the run of dry feed (Run 22). As mentioned earlier, the relative intensity of temperature excursion  $\Delta T$  reflects the adsorbed amount. An examination of Figure 6b shows that  $\Delta T$  at the prelayer increases with increasing feed water concentration; and correspondingly the front of the  $\Delta T$  curve proceeds from the F200/CDX interface (Run 19) further into the CDX middle layer (Run 20) and eventually reaches the layer interface of CDX/13X (Run 21). In the case of the highest feed humidity of 8.5% v/v (Run 21), a reasonable carbon capture performance was achieved: 58.2% recovery, 52.4% purity, and 0.128 kg CO<sub>2</sub>/h/L-adsorbent productivity, with such a single column triple-layered VSA and a simple three-step cycle. The employment of multicolumns and full process steps, such as product purge and pressure equalization, can further improve the overall performance.

# Effect of desorption time/vacuum level

During the evacuation step, water vapor and CO<sub>2</sub> are desorbed from the column along with the weakly adsorbed

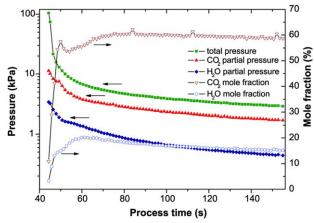


Figure 7. Pump down curve in terms of partial pressure and mole fraction during the 112 s evacuation step of CO<sub>2</sub>/H<sub>2</sub>O VSA (Run 12).

[Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

 $N_2$  and  $O_2$  and gases from the void spaces, where  $CO_2$  and  $H_2O$  mole fractions increase with decreasing partial pressures, for example, Run 12 with CDX/13X double-layered column. At the end of the desorption step, the  $CO_2$  partial pressure reaches 1.70 kPa and the  $H_2O$  partial pressure reaches 0.44 kPa (Figure 7). It must be pointed out that the  $CO_2$  concentration of the product stream increased after leaving the vacuum pump, because water vapor was condensed and trapped in the vacuum pump. In field applications, this water would be recovered by the liquid ring vacuum pump for other uses in a power plant.

Limited by the fixed feed conditions such as CO<sub>2</sub> concentration, flow rate, pressure, and step time in some of our experiments, the major parameters influencing the desorption are the evacuation time and consequently, the final vacuum pressure. Longer evacuation time provides a deeper vacuum level and enhanced CO<sub>2</sub> desorption as expected. As a result, the bed is cleaner and gives higher working capacity for CO2 and other weakly adsorbed gases (N2 and O2), which will subsequently contribute to larger amount of internal purge. Meanwhile, deeper vacuum level also means a larger volume of internal purge for the same amount of desorbed gas. This combined effect increases the P/F ratio (for fixed feed) and retains the water front in the prelayer. The water front moved further into the column as evacuation time decreased. In the worst case—80 s desorption, water already reached  $T_4$  (Z = 0.246), very close to the layering interface of CDX/13X. Consequently, the CO<sub>2</sub> product recovery and purity declined with further decrease of evacuation time and vacuum level (Figure 8a).

Using computer simulations, we can arbitrarily reduce the vacuum level while keeping the evacuation time constant, in order to investigate the separate effect of vacuum level. In Figure 8b, the wedge-shaped concentration wave of water vapor moved deeper into the column when the evacuation pressure was raised from 1 to 3 kPa. At a fixed feed concentration, the starting point of the concentration wave remained constant regardless of desorption conditions and only the slope of the wave decreased with the progression of the front. When the evacuation pressure was above 5 kPa, the front of water vapor became unbounded and tended to break

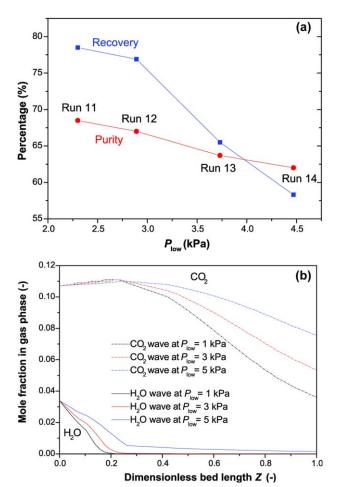


Figure 8. (a) CO<sub>2</sub> product purity and recovery for dry (Run 11) and wet CO<sub>2</sub> VSA (Run 12-14) with different desorption times and corresponding final vacuum pressures.

(b) Gas-phase water and  $CO_2$  distribution in the column at the end of the adsorption step, of simulation Run S1, S2, and S3. The feed gas contains 3.4% water and 10.7%  $CO_2$ . [Color figure can be viewed in the online issue, which is available at wileyonline library.com.]

through the entire column. Clearly, a lower vacuum level (higher  $P_{\rm Low}$ ) leads to a smaller P/F ratio and consequently, a longer water loaded zone.

# Effect of feed concentration

The feed concentration of the main adsorptives can greatly affect the feed and purge terms of the P/F ratio, and was investigated by our computer simulation (Table 2).

Reviewing the purge function, the total volume of purge gas  $V_P$  is the summation of the volume of desorbed  $CO_2$ , air, and  $H_2O$ , expressed as follows

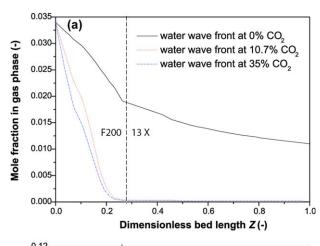
$$V_{\rm P} = V_{\rm P,CO_2} + V_{\rm P,air} + V_{\rm P,H_2O}$$
 (1)

where the main adsorptive  $CO_2$  takes up the majority of the total purge, and the carrier gas air and the secondary adsorptive  $H_2O$  take up the remainder.

The total volume of feed gas  $V_{\rm F}$  can be described similarly

$$V_{\rm F} = V_{\rm F,CO_2} + V_{\rm F,air} + V_{\rm F,H_2O}$$
 (2)

where the majority is the carrier gas air, the second largest fraction is  $CO_2$ , and the smallest fraction is  $H_2O$ . The



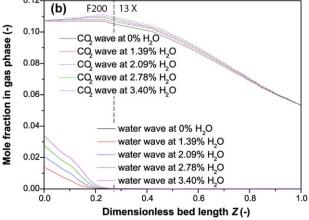


Figure 9. (a) Water wave in gas phase at various feed CO<sub>2</sub> concentration levels: 0% in S4, 10.7% in Run S2, and 35% in S5.

(b) Water and  $CO_2$  wave in gas phase at various feed  $H_2O$  concentration levels: 0% in Run S6, 1.39% in S7, 2.09% in S8, 2.78% in S9, 3.4% in S2. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

change of feed composition will not affect the total volume of feed gas  $V_{\rm F}$ , as the volumetric flow rate of the feed is constant, but it will affect  $V_P$ . By increasing the concentration of CO2 in the feed stream, the volume of desorbed CO2 increases accordingly, and the absolute value of  $V_P$  will increase. Therefore, the P/F ratio  $(V_P/V_F)$  will become larger. From Figure 9a, we can see that with zero CO<sub>2</sub> in feed nearly zero internal purge, water broke through the column immediately. With 10.7% CO<sub>2</sub> in feed, the concentration of water showed a repeated identical linear wave at the end of adsorption step of each cycle (not plotted) from cycle 100 to cycle 500, suggesting a stabilized front at CSS. Increase of CO<sub>2</sub> feed concentration from 10.7 to 35% increased the P/F ratio. However, the water front retreated only slightly at higher CO<sub>2</sub> feed (Figure 9a), which is consistant with our above experimental findings that further withdrawal of the water front is costly and less effective above the critical P/F

Here, the major constraint is that the recovery of water must be strictly 100% to prevent any breakthrough at CSS. Increasing water concentration in the feed will give higher  $V_{\rm P,H_2O}$  in Eq. 1. However, the net contribution to  $V_{\rm P}$  can be neutral or most likely, negative, considering that the amount

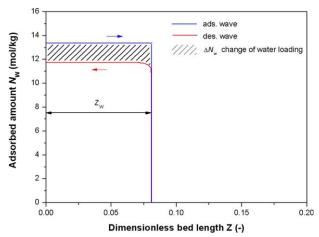


Figure 10. Anticipated solid phase concentration wave of water at the end of adsorption and desorption in Run 5.

of  $\mathrm{CO}_2$  recovered will decrease due to competitive adsorption of water. In Figure 9b, when the water concentration increased from 1.39 to 3.4%, the location of the water front only moved 20% forward, whereas the height of the water concentation wave was more than doubled. This indicates the increased amount of feed water concentration can be captured mainly by expanding the working capacity of the water occupied adsorbent layer, rather than further intruding the dry column layers proportionally.

#### Determination of water loaded zone

The ultimate aim of this work is to understand the penetration depth and distribution profile of water vapor inside the adsorption column and the subsequent effect on the carbon capture performance in the presence of water and, determine the forwards and backwards propagation of the water concentration front during the adsorption and desorption steps at CSS. The model developed below achieves these goals without undue complexity.

General Analytical Approach. At CSS, the amount of water fed into the bed equals the amount of water recovered by evacuation. This mass balance condition can be expressed as

$$\int_{0}^{Z_{\rm w}} (N_{\rm w.i} - N_{\rm w.f}) \frac{\pi D_{\rm in}^{2} \rho_{b} L}{4} dZ = \int_{0}^{t_{\rm f}} \frac{v_{\rm F} P_{\rm w}}{RT} dt \tag{3}$$

where the subscripts w, i, f, and F denote water component, initial, final and feed conditions, respectively. The right-hand side is the total water fed to the column during the feed step. Note that  $N_{\rm w}$  is a function of the local temperature and partial pressure of water. To solve Eq. 3, an axial distribution pattern of  $N_{\rm w}$  is indispensable, which can be obtained by either experimental measurement or computer simulation.

An analytical solution to this type of problem was attempted by Wilson et al.<sup>41</sup> in the case of O<sub>2</sub>VSA, with an approach similar to that by LeVan,<sup>40</sup> by assuming the adsorption front as a shock wave and the desorption front as a simple wave.<sup>47</sup> In that work, the velocity of the water front was characterized by a mass balance

$$\frac{dz}{dt} = \frac{v}{\varepsilon_t \left(1 + \frac{\rho_b RT}{\varepsilon_t} \frac{dN_w}{dP_w}\right)} \tag{4}$$

To locate the water loading profile at the end of the evacuation (and/or purge) step, an estimated length of water loaded zone is required and the solution to Eq. 4 is necessary. However, this approach heavily depends on detailed experimental or computer simulation data to determine the bed pressure as a function of time and to calculate the average gas velocity  $\nu$  and, it cannot provide straightforward expression of the minimum water penetration depth. Therefore, if it is solely for the purpose of determining the water front, the above technique would be no more accurate or convenient than the "cold spot" method or more sophisticated magnetic resonance imaging.  $^{48,49}$ 

As measurement of temperature change along the adsorption column is more convenient than that of concentration, by calculating the maximum temperature excursion at each thermocouple position along the column in a complete cycle at CSS, it is possible to estimate the dynamic working capacity of the adsorbate under adiabatic conditions during a single VSA cycle, that is,  $N_{\rm end~of~adsorption}-N_{\rm end~of~desorption}$ . Assuming the axial convection is negligible while ignoring gas-phase accumulation  $^{50}$  we get

$$\frac{dT}{dN} = \frac{\Delta H}{C_s} \tag{5}$$

which means the amount of adsorbate recovered by each node of the column in a cycle is proportional to the corresponding temperature change.

In the following parts, we demonstrate how to calculate the adiabatic working capacity by using the temperature profile. Once  $N_{\rm w.i}-N_{\rm w.f}$  is determined, the penetration depth of water  $Z_{\rm w}$  in the column can be resolved immediately from Eq. 3. Two typical patterns of water concentration wave will be investigated to understand the axial distribution of  $N_{\rm w}$  and ultimately, to determine the length of water loaded zone  $Z_{\rm w}$ .

Case I: Shock Wave Front and Adiabatic Conditions. As previously noted by LeVan<sup>40</sup> and Wilson et al.,<sup>41</sup> the adsorption front of water propagates as a shock wave because of the highly favorable adsorption isotherm of water on zeolite 13X (Supporting Information Figure S3b). Although the real wave front may be slightly dispersed, the assumption of a shock wave still remains a good approximation for water front in columns packed with materials having strongly favorable isotherms such as water on 13X.

The temperature change can be determined by calculating the difference between the temperatures at the end of adsorption and at the end of desorption steps. It was observed that the temperature change in the water loaded zone  $(\Delta T = 9.1^{\circ}\text{C} \text{ at } T_2 \text{ } (Z = 0.105) \text{ position and } \Delta T = 10.3^{\circ}\text{C} \text{ at}$  $T_3$  (Z = 0.175)) was almost even axially for Run 5, suggesting the amount of water removed by each node (axial working capacity  $\Delta N_{\rm Z}$ ) in a single cycle was of similar quantity. Therefore, we can anticipate the concentration profile of water remains in a shock wave during desorption, rather than a dispersive wave. However, the ratio of countercurrent purge amount (mainly by internal N<sub>2</sub>) to the amount of H<sub>2</sub>O desorbed is around 10:4 in our CO<sub>2</sub>VSA, approximately 8 times smaller than that in  $O_2VSA$  (~80:4). Practically, in a PSA process, the purge amount can be increased by adding extra external purge gases (e.g., product purge). In this work,

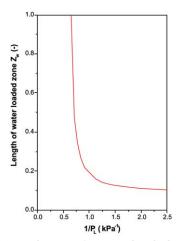


Figure 11. Dependence of water loaded zone on the reciprocal of water partial pressure  $P_{\text{L,H}_2\text{O}}$  in 13X single-layer column with 97.4% RH feed at 30°C.

we will also adopt the "frozen front" theory<sup>41</sup> that the foremost edge of the water front stabilizes at CSS due to its strongly favorable isotherm shape. The cyclic water adsorption/desorption concentration curves are illustrated in Figure 10.

Based on the shock wave trajectory (Figure 10), the term on left-hand side of Eq. 3 can be simplified as

$$\int_{0}^{Z_{\rm W}} (N_{\rm w.i} - N_{\rm w.f}) \frac{\pi D_{\rm in}^{2} \rho_{b} L}{4} dZ = \Delta N_{\rm w} \frac{\pi D_{\rm in}^{2} \rho_{b} L}{4} Z_{\rm w}$$
 (6)

$$\Delta N_{\rm w} = N_{\rm w}(P_{\rm H}, T_{\rm H}) - N_{\rm w}(P_{\rm L}, T_{\rm L})$$
 (7)

where  $\Delta N_{\rm w}$  is the working capacity of water on the adsorbent in the given partial pressure envelope of  $P_{\rm H} \to P_{\rm L}$  and the temperature range. For isothermal processes, this value can be directly calculated from the isotherm equations, whereas under nonisothermal conditions, the determination is not straightforward, as the loading is coupled with the temperature change. We consider an adiabatic process in this study, given the relatively large diameter (5 cm) of the column and good thermal insulation around the column. Therefore, the adiabatic working capacity of water  $\Delta N_{\rm w}$  can be derived explicitly from the isobaric diagram (Supporting Information Figure S4) or by integration of the total differential of the isotherm equation as a function of T and P in Eq. 5 as follows

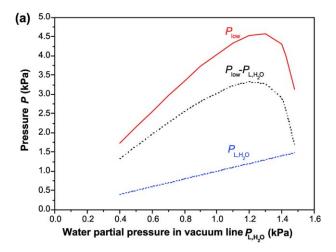
$$\int_{N_{L}}^{N_{H}} \Delta H(P,T) dN = C_{s} (1 + N(P_{L}, T_{L})) T_{H}$$

$$-C_{s} (1 + N(P_{H}, T_{H}) M) T_{L}$$
(8)

where the left-hand side is the integral heat from loading  $N_{\rm L}$  at low pressure and low temperature to loading  $N_{\rm H}$  at high pressure and temperature. M denotes the molecular weight of adsorbate and the heat capacity of adsorbate is assumed same as that of the adsorbent  $C_s$ .

For systems with constant isosteric heat, for example, single-site Langmuir or linear isotherms, the above equation becomes

$$\frac{N(P_{\rm H}, T_{\rm H}) - N(P_{\rm L}, T_{\rm L})}{(1 + N(P_{\rm L}, T_{\rm L})M)T_{\rm H} - N(P_{\rm H}, T_{\rm H})MT_{\rm L}} = \frac{C_s}{\Delta H}$$
(9)



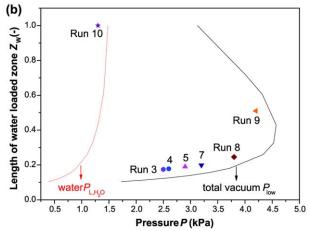


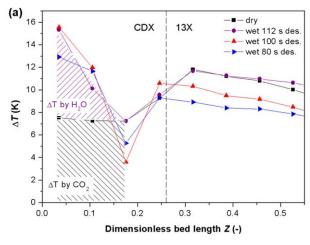
Figure 12. (a) The dependence of the lowest total vacuum pressure  $P_{\text{low}}$  on the lowest partial pressure of water vapor in the vacuum line  $P_{\text{L,H}_2\text{O}}$ ; and (b) the dependence of the length of water loaded zone  $Z_{\text{W}}$  on the lowest vacuum pressure of the system  $P_{\text{low}}$  in 13X single-layer column with 97.4% RH feed at 30°C.

Lines are predicated results by our simple model and solid symbols are experimental data points as a function of  $P_{\rm low}$  of individual runs. All the data are calculated/measured at 30°C except for Run 10. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

There are four variables in Eq. 8, namely  $P_{\rm H}$ ,  $P_{\rm L}$ ,  $T_{\rm H}$ , and  $T_{\rm L}$ , and they vary along the bed. At the inlet of the bed,  $P_{\rm H}$  and  $P_{\rm L}$  are normally known for a given VSA. At the end of adsorption step,  $T_{\rm H}$  is higher than the feed temperature  $T_{\rm F}$ , whereas at the end of desorption step  $T_{\rm L}$  is lower than  $T_{\rm F}$ , and they swing across  $T_{\rm F}$  with approximately equal amplitude (e.g., Supporting Information Figure S2). It is important to note that  ${\rm CO_2}$  physisorption on water loaded 13X zone is negligible, so the temperature swing in water loaded 13X zone can be attributed to  ${\rm H_2O}$  adsorption/desorption only. The following assumption is made

$$\frac{T_{\rm H} + T_{\rm L}}{2} = T_{\rm F} \tag{10}$$

The physical meaning of Eqs. 8 and 10 is that at given pressure envelop and feed temperature, the adiabatic



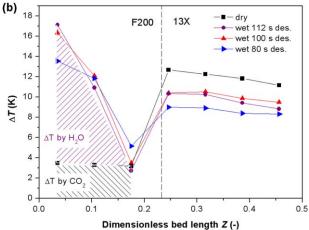


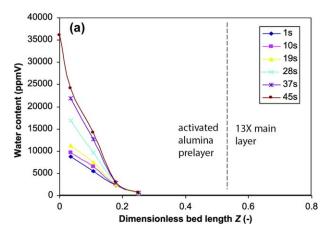
Figure 13. Temperature changes in the double-layered columns measured by individual thermocouples in a single cycle at CSS for dry CO<sub>2</sub> feed, and for wet feed with different desorption time: 112, 100, and 80 s.

(a) CDX/13X layering of Run 11-14; (b) F200/13X

(a) CDX/13X layering of Run 11–14; (b) F200/13X layering of Run 15–18. [Color figure can be viewed in the online issue, which is available at wileyonline library.com.]

adsorption working capacity of the specific adsorbent is fixed. Combining Eqs. 8 and 10, we can determine the adiabatic working capacity of water  $\Delta N_{\rm w}$  by Eq. 7. By substituting  $\Delta N_{\rm w}$  into Eq. 6 and then Eq. 3, eventually, the length of water loaded zone is obtained.

Using the experimental conditions of Run 5, for example,  $P_{\rm H} = 3.48 \text{ kPa}, P_{\rm L} = 0.63 \text{ kPa}, \text{ and } T_{\rm F} = 303.15 \text{ K}, \text{ the length}$ of the water layer was determined as 0.125. It must be clarified that  $P_{\rm L}$  represents the lowest partial pressure of water in vacuum line rather than the overall lowest vacuum pressure  $P_{\text{low}}$  in Table 1. By manipulating  $P_{\text{L}}$ , we can generate a range of data as plotted in Figure 11. The horizontal axis was cast into  $1/P_L$  rather than  $P_L$  for comparison with Figure 3a because the volumetric flow rate is inversely proportional to  $P_{\rm L}$ . The predicted results by our model (Figure 11) show a similar trend of water loaded length to experimental measurements (Figure 3a). The water front stays steady at the bottom of the column at appropriately deep vacuum. However, further deepening the vacuum will not effectively reduce the water loaded length but requires more pump work, as later suggested by comparing the energy consump-



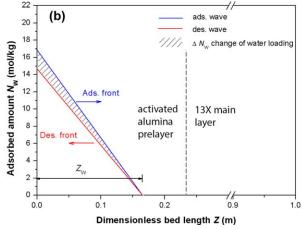


Figure 14. (a) Propagation of water concentration wave in gas phase during the adsorption step at CSS in Run 19.

(b) An illustration of the solid phase water wave front model for a typical activated alumina CDX + 13X column at CSS by using operation conditions of Run 12. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

tion of Run S1 and S2. Herein, a critical vacuum level of water vapor exists, approximately within the range of  $0.8 < P_{\rm L} < 1$  kPa—analogous to the forementioned critical P/F, above which the water front tends to break through the column. The predicted water loaded length is slightly shorter than the experimental one (Run 5), probably because local equilibrium was used in the model without considering the impact of kinetics and also the real water concentration wave may have some degree of dispersion. Incorporation of a shrinking core model may better account for the kinetic effects.  $^{51}$ 

In a field VSA unit, determination of the lowest total pressure  $P_{\rm low}$  in the vacuum line is critial in selection of the vacuum pump and estimation of the energy consumption of the process which is often reflected in terms of compression ratio  $P_{\rm high}/P_{\rm low}$ . Therefore, it is essential to find the relationship between the length of water loaded zone  $Z_{\rm w}$  and the lowest pressure  $P_{\rm low}$  of the system, when the pressure envelop of water vapor is given. As the dependence of water loaded zone  $Z_{\rm w}$  on the lowest partial pressure of water  $P_{\rm L,H_2O}$  is known from the above analysis (where  $P_{\rm L,H_2O}$  was cited as  $P_{\rm L}$ ), we can easily find the relationship between  $P_{\rm L,H_2O}$  and  $P_{\rm low}$ , by taking mass conservation and some

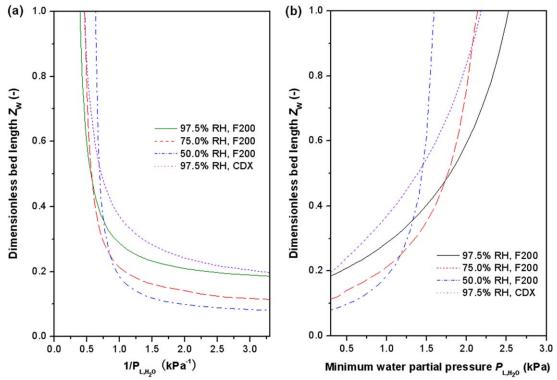


Figure 15. Dependence of water loaded zone, (a) on the reciprocal of water partial pressure, and (b) on water partial pressure, in the prelayer of activated alumina F200 and CDX, respectively.

appropriate assumptions (see Supporting Information). The total vacuum pressure can be estimated as follows

$$P_{\text{low}} = P_{\text{L,H}_2\text{O}} \frac{N_{\text{F,H}_2\text{O}} + N_{\text{F,CO}_2} R_{\text{CO}_2,\text{dry}} \left(1 - Z_{\text{w}} + \frac{1 - \varphi_{\text{CO}_2,\text{dry}}}{\varphi_{\text{CO}_2,\text{dry}}}\right)}{N_{\text{R,H}_2\text{O}}} \quad (11)$$

where  $R_{\rm CO_2,dry}$  denotes the  $\rm CO_2$  recovery obtained from the corresponding runs with dry feed and  $\varphi$  denotes the purity of recovered  $\rm CO_2$ .

We applied this model to the case of a shock wave water front (Run 3-10) by using dry gas feed Run 2 as reference for Eq. 11. We obtained the comparison between the lowest partial pressure of water vapor in the vacuum line  $P_{L,H_2O}$ and the lowest total vacuum pressure  $P_{low}$  in terms of their influence on the length of water loaded zone  $Z_{\rm W}$ . In Figure 12a,  $P_{\text{low}}$  first increases with  $P_{\text{L,H}_2\text{O}}$  when  $P_{\text{L,H}_2\text{O}} < 1.3$  kPa, and then  $P_{\text{low}}$  drops suddenly with the increase of  $P_{\text{L,H},\text{O}}$ when  $P_{L,H_2O} > 1.3$  kPa. The difference between  $P_{low}$  and  $P_{L,H_2O}$ , that is,  $P_{low}-P_{L,H_2O}$ , which is the contribution of desorbed CO2 and other inert components into the vacuum line, drops even more drastically at  $P_{L,H_2O} > 1.3$  kPa. The underlying physical meaning is that with increase of partial pressure of water in the vacuum line, for example, due to shortened desorption time or loss of pump capacity, the length of remaining dry zeolite layer (1-Z<sub>W</sub>) used for CO<sub>2</sub> capture is being dramatically shortened (Figure 12b, dashed curve) leading to less recovery of CO<sub>2</sub>. As the loss of CO<sub>2</sub> is much more than the increase of water vapor under evacuation when  $P_{L,H_2O} > 1.3$  kPa, the total vacuum pressue  $P_{low}$ decreases while water vapor tends to break through the column, as illustrated by the solid curve in Figure 12b. The inflection point of this curve corresponds to the transformation of the process from a CO<sub>2</sub>/H<sub>2</sub>O VSA to a water VSA predominantly. This unusual interdependent relationship between  $Z_{\rm w}$  and  $P_{\rm low}$  is supported by our experimental observation (data points in Figure 12b).

Case II: Linear Dispersive Wave Front. From Figure 13, we can see that in the case of dry  $CO_2$  feed, there were two  $\Delta T$  plateaus with the one in the 13X layer higher than the one in the prelayer. That indicates the recovered amount of  $CO_2$  was uniform in each layer within the displayed scale but differentiates across the layer boundary. After the introduction of water, the plateau in the 13X layer was not significantly altered.

It is known that the loading of CO<sub>2</sub> on activated alumina (F200) in the binary system is low but almost unchanged due to the enhancement effect by cooperative adsorption of H<sub>2</sub>O, in which CO<sub>2</sub> was believed to have a secondary adsorption on adsorbed water layers by forming complexes with water molecules.<sup>52</sup> Therefore, the temperature change in the alumina prelayer as shown in Figure 13 (wet 112 s desorption) can be attributed to the summation of  $\Delta T$  by  $CO_2$  (square shaded area) and  $\Delta T$  by  $H_2O$  (triangle shaded area). It can be also observed from Figure 13 that  $\Delta T$  by CO<sub>2</sub> is the same for both dry and wet runs (112 s desorption). Subtracting the contribution of  $\Delta T$  by CO<sub>2</sub> (this value varies with different operation conditions accordingly), we can find the reversible adsorption/desorption amount of H2O on activated alumina prelayer decrease quasilinearly along the axial direction.

Apart from the linear  $\Delta T$  profile, there are direct evidences from experiments (Figure 5) and simulations (Figures 9a and 10) in which the gas-phase water concentration front can be approximated by a wedge-shaped linear wave. In our latest VSA experiments with F200/CDX/13X triple-layered bed configuration (Run 19), we found that during the feed step

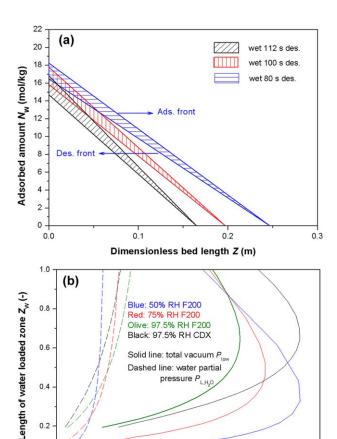


Figure 16. (a) Predicted adsorption/desorption wave front of water concentration in solid phase in Run 12 ( $P_{low} = 2.89$  kPa), 13 ( $P_{low} = 3.73$  kPa), and 14 ( $P_{low} = 4.47$  kPa).

Pressure P (kPa)

The results are comparable to the experimental data in Figure 11. The three shaded areas are of the same size. (b) The dependence of the length of water loaded zone  $Z_{\rm W}$  on the lowest vacuum pressure of the system  $P_{\rm low}$  (solid line) in comparison with that on the lowest water partial pressure  $P_{\rm L,H_2O}$  (dashed line), in activated alumina/13X double layer column with a range of RH feed at 30°C. The prelayer adsorbent was alumina F200 and alumina CDX, respectively. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

the wedge-shaped wave propagated in a manner that only the slope of the wave increased with time but the foremost edge remained frozen (Figure 14a). We believe the wedge-shaped water concentration wave is a result of the nature of the quasilinear water isotherm (Supporting Information Figure S3b) and the effect of cyclic forwards/backwards gas flow in the column. It implies that the axial distribution of the amount of water removed per cycle by activated alumina prelayer can be approximated by a "triangle" or "wedge" configuration as illustrated by the shaded area in Figure 14b, where the amount of water removed at each node  $\Delta N_{\rm w}$  decreases linearly along the column.

At CSS, the amount of water removed by the prelayer equals the amount of water fed to the column, the general analytical approach described by Eq. 3 is valid. The left side of Eq. 3 can be expressed as

$$\int_{0}^{Z_{W}} (N_{w.i} - N_{w.f}) \frac{\pi D_{in}^{2} \rho_{b} L}{4} dZ = \Delta N_{w} \frac{\pi D_{in}^{2} \rho_{b} L}{8} Z_{w}$$
 (12)

which is the modified version of Eq. 6 for characterising axial working capacity with "triangle" configurations. By assuming adiabatic operation and validation of the simple energy balance Eq. 5, we can use the same approach in Case I to determine the adiabatic working capacity of water  $\Delta N_{\rm w}$  (Eqs. 8 and 10). The isotherm equations of water on corresponding materials are available from our previous study. 52,53 In addition, the impact of coadsorbed CO2 on water adsorption is negligible. Substituting  $\Delta N_{\rm w}$  into Eq. 12 will give the length of water loaded zone. We use experimental conditions of Run 12  $(P_{L,H_2O} = 0.4346 \text{ kPa})$  and Run 16  $(P_{L,H_2O} = 0.444 \text{ kPa})$  as input information for the above model and the calculated results are demonstrated in Figure 15. The general trend of the water loaded length in activated alumina prelayers against the reciprocal of the  $P_{L,H_2O}$  of water vapor is not as steep as that in the single-layered 13X column (Figure 11), which means the processes using activated alumina prelayers are more robust at varing humidities. From Figure 15, it can be seen that under the same operating conditions, compared with F200 prelayer, a thicker prelayer of CDX is required to prevent water penetration into the main layer; above the critical  $1/P_{L,H_2O}$ , lower feed relative humidity will generate a shorter water zone. However, the critical 1/P<sub>L,H,O</sub> decrease with rising feed water content, indicating even smaller partial pressure of water vapor  $P_{\rm L.H_2O}$ is required to cope with lower feed relative humidity. This feature is of particular concern in the case of a liquid ring vacuum pump whose vacuum level is limited by the saturation pressure of the working fluid, imposing a risk of process failure in hot weather. However, the deficiency of the vacuum pump can be possibly compensated by the large amount of internal purge gas (mainly CO<sub>2</sub>) which can substantially reduce the partial pressure of H<sub>2</sub>O (Figure 7) in the case of high concentration CO<sub>2</sub> in feed, for example, 35% CO<sub>2</sub> in Run S5, Figure 9a. Conversely, shorter evacuation time will lead to higher  $P_{L,H_2O}$ and smaller  $\Delta N_{\rm w}$ , and thus the water front will propagate further into the bed as expected (Figure 16a). By applying Eq. 11 to the multilayered VSA runs, the interdependent relationship between the deepest vacuum pressure  $P_{low}$  and the penetration dependence of water vapor in the column  $Z_{\rm w}$  can be determined, as shown in Figure 16b. At low  $Z_w$  range,  $Z_w$  increases with  $P_{\text{low}}$ , whereas in the high  $Z_{\text{w}}$  range  $P_{\text{low}}$  becomes even smaller. This special feature is very similar to what we have discussed earlier in the single-layered column (Figure 12) and the underlying mechanism is same. By comparing the curve of total vacuum pressure  $P_{\rm low}$  in Figure 16b with that in Figure 12, we can see that the column using an activated alumina prelayer can tolerate a larger  $P_{low}$  pressure than the one without prelayer. This means the adoption of a water removal prelayer can potentially save a considerable amount of vacuum pump in a CO<sub>2</sub>/H<sub>2</sub>O VSA process. Therefore, the partial pressure of water vapor in the vacuum line  $P_{L,H_2O}$  is a function of pump capacity, internal purge, and evacuation time. The dimensionless water loaded length is independent of the feed step time or the absolute bed length but depends on the feed composition, temperature, and evacuation pressure which are practically covered by the purge-to-feed ratio, as well as the physical properties of the adsorbents, such as isotherm shape, heat capacity, bulk density and so forth. Therefore, the optimal ratio of "prelayer-to-main layer"— $\lambda$  is defined as the ratio between the length of the two layers when CO<sub>2</sub> is recovered at an appropriate purity and recovery by the main layer (as determined from dry CO<sub>2</sub> VSA, e.g., Run 2) and meanwhile H<sub>2</sub>O is just exactly 100% recovered by the prelayer without any unused bed length and this ratio can be formulated as follows

$$\lambda = \frac{Z_{\rm w}}{1 - Z_{\rm w}} \tag{13}$$

In real operations,  $\lambda$  should be determined by taking into account the most conservative circumstances with some safety margin.

## **Conclusions**

In this study, we have demonstrated that CO<sub>2</sub> can be effectively captured from highly humid postcombustion flue gases by VSA with multilayered columns. Activated alumina F200 and CDX are good candidates for the prelayer adsorbents because of their quasilinear water isotherms which endow them with higher working capacities under VSA conditions, while zeolite 13X still remains one of the best commercial adsorbents for carbon capture in the main layer. Our experiments and computer simulations suggests the key factors controlling the performance of the CO<sub>2</sub>/H<sub>2</sub>O VSA process are volumetric purge-to-feed ratio and layering strategy of the adsorbents.

The volumetric P/F ratio has been examined for VSA processes particularly with little external purge. Water can be successfully removed along with the CO<sub>2</sub> stream by maintaining an appropriate volumetric P/F ratio, where the water front stabilizes in the bed. However, when the P/F ratio is lower than the critical value, water tends to penetrate the column and there is a high risk of process failure. The volumetric P/F ratio is a lumped parameter capturing the effects of feed and evacuation conditions. The feed CO<sub>2</sub> concentration, evacuation time, and vacuum level contribute positively to the P/F ratio, whereas feed H<sub>2</sub>O concentration impacts negatively. Of particular importance, dry CO<sub>2</sub> desorbed from the main layer plays a role of internal purge, which is essential to lowering the water partial pressure during the evacuation step and the relatively hotter CO2 gas also brings the heat from the main layer of the column to facilitate the desorption of water in the prelayer.

The length of water loaded zone is a major criteria to evaluate the effectiveness of water removal by the prelayers. We developed an axial adiabatic working capacity model to estimate the penetration depth of water in the column, based on a simple mass and energy blance using an analytical approach. The model has been successfully applied to two types of water wave fronts: (1) shock wave for adsorbents with sharp Type I isotherms; (2) linear dispersive wave for materials with linear or quasilinear isotherms. It was predicted by the model that the length of the water loaded zone increased exponentially with the elevation of the lowest partial pressure of water  $(P_L)$  in the vacuum line, suggesting the existance of a critical  $P_L$  above which the water front becomes unbounded. As  $P_L$  is normally a preset operation constraint, the length of water loaded zone can be resolved by the model and then, the required minimum layering ratio (prelayer:main layer) can be determined. The layering ratio is of particular importance in designing a layered column at given operation conditions.

For low to medium humidity feed, double-layered columns are more effective than single-layered ones in terms of  $\rm CO_2$  capture. However, at high humidity (>8.5% v/v), reasonably good performance can be achieved with our strategy of novel

triple-layered column by maximizing the efficiency of the adsorbents-making the first prelayer dedicated to water removal, the second prelayer effective for water and CO2, and the main layer targeted for CO<sub>2</sub>. Extrapolation of this process to multicolumns and full process steps. To further reduce the capture cost, system integation is also possible for industrial scale capture process by means of: (1) heat integration, such as recovering the high exergy contained in the massive CO<sub>2</sub>-removed dry flue gases from the VSA units, for example, brown coal drying and adsorbents regeneration; (2) materials recycle, such as making use of the large amount of liquid water collected by the vacuum pump. The ultimate strategy to solve the detrimental effect of H<sub>2</sub>O is to use water tolerant/hydrophobic CO2 adsorbents. However, the development of such materials is extremely challenging.

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#### **Notation**

c = gas-phase concentration, mol/m3

 $\overline{c}$  = instantaneous gas-phase concentration, mol/m3

 $C_s$  = sorbent heat capacity, kJ/kg K

CDX = a type of activated alumina

CSS = cyclic steady state

 $D_{\rm in}$  = inner diameter of the adsorption column, mm

F200 = a type of activated alumina, same as F-200

 $\Delta H$  = heat of adsorption, kJ/kg

K = LDF coefficient, 1/s.

K = Henry law constant

L =length of the adsorbents in column, m

LDF = linear driving force

MINSA = Melbourne integrated numerical simulator for adsorption

N = adsorbed amount, mol/kg

P = pressure, kPa or bar

 $P_{\rm L}$  = the lowest partial pressure of a component (H<sub>2</sub>O) in evacua-

tion step, kPa

 $P_{L,H_2O}$  = the lowest partial pressure of water vapor in evacuation step, kPa

 $P_{\text{low}}$  = the lowest total pressure in evacuation step, kPa

ppm = part per million

PSA = pressure swing adsorption

P/F = purge to feed ratio

R = gas constant, J/mol/K

RH = relative humidity

 $T = \text{temperature}, ^{\circ}\text{C}$ 

v = volumetric flow rate, m3/s

VSA = vacuum swing adsorption

y = mole fraction in gas phase

Z = dimensionless bed distance

#### Greek letters

 $\varepsilon$  = voidage

 $\lambda$  = layering ratio

M = molecular mass, g/mol

 $\rho = \text{density, kg/m}^3$ 

 $\varphi = \text{purity}$ 

# Subscripts and superscrits

b = bed

f = final state

F = feed

H = high

i = initial state

in = inlet L = low

out = outlet P = purge

R = recovered

s =solid phase

t = total

w = water

\* = equilibrium state

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